

FRONTIERS ARTICLE

Statistical mechanics of sum frequency generation spectroscopy for the liquid–vapor interface of dilute aqueous salt solutions

Joyce Noah-Vanhoucke^a, Jared D. Smith^b, Phillip L. Geissler^{a,b,*}^a Department of Chemistry, University of California, Berkeley, CA 94720, United States^b Chemical Sciences Division Lawrence Berkeley National Lab, Berkeley, CA 94720, United States

ARTICLE INFO

Article history:

Received 3 January 2009

In final form 5 January 2009

Available online 19 January 2009

ABSTRACT

We demonstrate a theoretical description of vibrational sum frequency generation (SFG) at the boundary of aqueous electrolyte solutions. This approach identifies and exploits a simple relationship between SFG lineshapes and the statistics of molecular orientation and electric field. Our computer simulations indicate that orientational averages governing SFG susceptibility do not manifest ion-specific shifts in local electric field, but instead, ion-induced polarization of subsurface layers. Counterbalancing effects are obtained for monovalent anions and cations at the same depth. Ions held at different depths induce an imbalanced polarization, suggesting that ion-specific effects can arise from weak, long-ranged influence on solvent organization.

© 2009 Elsevier B.V. All rights reserved.

1. Introduction

Interest in ion solvation at interfaces has been renewed by recent developments in nonlinear spectroscopic experiments (notably sum frequency generation and second harmonic generation), as well as computer simulation studies that point to unexpected aqueous surface phenomena for simple inorganic anions. Specifically, these simulations suggest that large atomic anions, such as iodide, experience an effective attraction for the liquid–vapor interface [1–5], counter to predictions from cornerstone theories of ion solvation in bulk water [6,7]. Although a growing number of experimental studies support this surprising notion of surface enhancement [8–11], detailed inferences from the data rest on methods that remain controversial [12].

Sum frequency generation (SFG) is the only second-order optical process that provides information on the vibrational response of molecules at an interface. Detailed theoretical formulations permit calculation of SFG intensity, e.g., for liquid–vapor interfaces, from computer simulations [13–17], but do not by themselves offer a transparent physical picture of its relationship to intermolecular structure. We have recently presented a convenient, albeit approximate, approach to such calculations for the specific case of hydroxyl stretching at aqueous liquid–vapor interfaces. By neglecting solvent dynamics and casting the influence of a proton's surroundings as a Stark effect, it reduces SFG susceptibility to a superposition of simple orientational averages resolved by fluctuations in electric field [18]. These approximations, which underlie

very accurate theories of Raman spectra for bulk aqueous solutions [19,20], clarify the spectroscopic consequences of molecular alignment and distortions of intermolecular arrangements near the liquid surface. In particular, they highlight the weakness of orientational bias for interfacial molecules that donate hydrogen bonds [18].

In this work, we apply such a computational approach to the liquid–vapor interface of salt water. Specifically, we consider the influence of dissolved halide anions and sodium cations on hydroxyl stretching of dilute HOD solutes in D₂O solvent. Section 2 reviews the orientational averages that govern resonant SFG susceptibility within our approximations. Our numerical methods are described in detail in Section 3, and results of molecular dynamics simulations are presented in Section 4. These calculations identify those aspects of interfacial ion solvation that strongly determine spectroscopic observables. They suggest that ion-specific effects may, in fact, be closely related to spontaneous charge layering at the interface.

The polarizability of larger atomic anions, such as iodide, has been assigned a central role in the disputed phenomenon of aqueous surface adsorption [3–5]. For ease of interpretation, we focus attention in this paper on results for model ions that lack polarizability, but are held at fixed depth. In doing so, we anticipate that the direct spectroscopic influence of induced solute dipoles need not be as significant as is their impact on the ions' spatial distribution. In Section 4.2 we present results for polarizable ion models that confirm this expectation. These calculations were performed by an exact reweighting of data obtained from non-polarizable models, as we will describe in detail.

We conclude in Section 5 with a discussion of the implications of our results for interpreting SFG spectra of electrolyte liquid–vapor interfaces.

* Corresponding author. Address: Department of Chemistry, University of California, Berkeley, CA 94720, United States.

E-mail address: geissler@berkeley.edu (P.L. Geissler).

2. Orientational averages responsible for SFG

SFG response is proportional to the squared magnitude of the second-order susceptibility χ , which in turn is proportional to the average molecular hyperpolarizability, $\chi \propto \langle \beta \rangle$. The theory developed in Ref. [18] emphasizes the importance of orientational averages of the form $\langle j_x k_y l_z \rangle_{\mathcal{E}}$ in determining the absorptive part of SFG susceptibility. Here, j_x , k_y , and l_z are projections of the Cartesian unit vectors \mathbf{j} , \mathbf{k} , and \mathbf{l} defining a water molecule's reference frame onto the α , γ , and ζ axes of the laboratory frame. Averages $\langle \cdot \rangle_{\mathcal{E}}$ for an HOD molecule are conditioned on the solution's electric field \mathcal{E} evaluated at the proton's position and projected onto the OH bond. Within our approximations, variations in hydroxyl stretching frequency are directly proportional to this fluctuating electrostatic coordinate, $\omega = \omega^{(0)} + Q\mathcal{E}$, where Q and $\omega^{(0)}$ are positive constants [21,22].

For the most widely used combination of input light polarizations, *ssp*, our estimate for the imaginary part of the resonant hyperpolarizability is given by

$$\text{Im} \beta_{\text{xxx}}^{(\text{R})}(\omega) = \frac{\pi}{Q} P(\mathcal{E}) \sum_{j,k,l} \alpha'_{jk} \mu'_l \langle j_x k_x l_z \rangle_{\mathcal{E}}, \quad (1)$$

where the laboratory z -axis points outward from and normal to the liquid's surface. The superposition of orientational averages in Eq. (1) is weighted by the probability distribution over the entire system, $P(\mathcal{E})$, which is overwhelmingly dominated by contributions from the slab's bulk-like interior. The frequency-independent coefficients $\alpha'_{jk} \mu'_l$ are determined by matrix elements of the dipole and polarizability derivatives with respect to the vibrational coordinate. See Ref. [18] for a detailed account of this expression's origin and for precise definitions of the constant parameters involved. (see Table 1).

The conditional averages $\langle j_x k_x l_z \rangle_{\mathcal{E}}$ quantify the correlation between a molecule's hydrogen bonding environment, as characterized by \mathcal{E} , and its orientational bias due to the interface. Of the 18 distinct choices of the set $\{j,k,l\}$, eight are zero due to symmetry. Of the remaining ten choices, four are negligible due to the likely very small values of α'_{jk} and μ'_l that multiply them. The final six are significantly redundant in their frequency dependence. They can each be written, to a good approximation, as a linear combination of the simpler averages $\langle u_z \rangle_{\mathcal{E}}$ and $\langle u'_z \rangle_{\mathcal{E}}$, where \mathbf{u} and \mathbf{u}' denote unit vectors along the OH and OD bonds, respectively, of an HOD molecule.

The essence of an SFG lineshape in our approach thus reduces to two functions of electric field (or, equivalently, frequency), each

Table 1
Table of important variables used throughout the paper.

z	Cartesian coordinate in the direction normal to the liquid–vapor interface relative to the liquid's center of mass
z_{ion}	Position of an ionic solute in the z -direction
z_{Gibbs}	Position of the Gibbs dividing surface, i.e., half of the thickness of the liquid slab
Δz_{ion}	Position of an ionic solute relative to the Gibbs dividing surface, i.e., $z_{\text{ion}} - z_{\text{Gibbs}}$
\mathcal{E}	Instantaneous electric field generated by the solution, evaluated at the proton's position and projected onto the corresponding hydroxyl bond
$P(\mathcal{E})$	Probability distribution of \mathcal{E} at thermal equilibrium
\mathbf{u}, \mathbf{u}'	Unit vectors in the HOD molecular reference frame, pointing along the OH and OD bond directions, respectively
u_z, u'_z	Projections of the unit vectors \mathbf{u} and \mathbf{u}' onto the outward surface normal of the liquid slab
$\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$, $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$	Conditional averages of u_z and u'_z for hydroxyl groups with a given value of \mathcal{E} , when an ion is located at height z_{ion}
ξ_{ion}	Instantaneous electrostatic force per unit charge exerted by the solution on an ionic solute, in the z -direction

multiplied by the electric field distribution $P(\mathcal{E})$. The first, $\langle u_z \rangle_{\mathcal{E}}$, quantifies the orientation of OH bonds whose protons experience a given electric field \mathcal{E} . The second, and slightly more subtle, $\langle u'_z \rangle_{\mathcal{E}}$, quantifies the orientation of OD bonds whose corresponding protons experience a particular value of \mathcal{E} . The effect of dissolved ions on SFG follows from changes in these two functions. The distribution $P(\mathcal{E})$ of electric field fluctuations over the entire slab is extremely insensitive to their presence and location at the ionic strengths we consider. Our simulations consider different ranges of ion depth separately. Because these ranges are narrow, we effectively compute orientational averages $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ conditioned not only on electric field, but also on the ion's vertical coordinate, z_{ion} .

3. Simulation methods

We have investigated the SFG response of dilute HOD in D₂O for a series of electrolyte solutions consisting of either one or two ions dissolved in water. In particular, we simulated the dynamics of $N = 512$ molecules interacting via the SPC/E potential [23] computed with Ewald sums, at ambient temperature and at fixed densities that enforce liquid–vapor coexistence. The system consists of a slab of liquid with two air–liquid interfaces. The slab dimensions are $20 \text{ \AA} \times 20 \text{ \AA} \times 40 \text{ \AA}$ with nearly 60 \AA of vapor in the z -direction. The box dimensions are $L_x \times L_y \times L_z = 20 \text{ \AA} \times 20 \text{ \AA} \times 100 \text{ \AA}$. Statistics were accumulated for the positive, $z > 0$, half of the slab system, where the z -coordinate of the hydrogen atom was used to determine to which half of the slab a particular OH group belongs. The procedure for creating this interfacial system, the implications of our symmetry breaking convention, and further aspects of our simulation methodology are described in greater detail in Ref. [18]. Interactions between ions and water and between different ions were computed according to models developed by Dang and coworkers [24] (absent contributions due to molecular and ionic polarizability). Our simulations explored only Na⁺ as the cation species, and several halide anions: F[−], Cl[−], Br[−], and I[−]. Single-ion systems are, in principle, unstable due to interactions between periodic images that are not electroneutral. By neglecting the zero-wavevector contribution in Ewald sums, we effectively stabilize these systems by introducing a uniform neutralizing background charge density of opposite sign.

Molecular dynamics simulations were performed using the LAMMPS software package [25]. The SHAKE algorithm [26] was used to maintain rigid molecular geometries in these calculations. Equilibration runs employed a Nosé–Hoover thermostat [27] for at least 200 ps, while production runs were propagated by integrating Newton's equations of motion using the velocity Verlet algorithm [28] for at least 2 ns. In both cases $\Delta t = 1 \text{ fs}$ served as the fundamental time step of integration.

Ions, when present without a partner counterion, were allowed to explore limited ranges of depth $\Delta z_{\text{ion}} = z_{\text{ion}} - z_{\text{Gibbs}}$, where z_{Gibbs} is the value of z at which the solvent density falls to half its bulk value. This biasing of the ion position was achieved via an external potential,

$$U_{\text{bias}} = u_0 (z_{\text{ion}} - \bar{z} - z_0)^4, \quad (2)$$

where

$$\bar{z} = \frac{\sum_{i=1}^N z_i^{(0)} h(z_i^{(0)})}{\sum_{i=1}^N h(z_i^{(0)})} \quad (3)$$

is an effective center of mass for the slab. The counting function $h(z) = (1 + \exp[a(z - L_z/2)])^{-1} \times (1 + \exp[-a(z + L_z/2)])^{-1}$, with $a =$

4 \AA^{-1} , smoothly restricts the center of mass calculation to the central simulation cell. The summations run over all molecules in the system, and the superscripts (O) indicate that a molecule's position is determined by its oxygen atom's location. By choosing $u_0 = 0.5 \text{ kcal/mol \AA}^4$ we were able to restrict an ion's motion in the z -direction to within $\pm 1 \text{ \AA}$ of z_0 . Simulations were performed for a series of ion depths: $z_0 = 0, 9 \text{ \AA}, 11 \text{ \AA}, 13 \text{ \AA}, 15 \text{ \AA}, 17 \text{ \AA}, 19 \text{ \AA}$, and 21 \AA (corresponding roughly to $\Delta z_{\text{ion}} \approx -20 \text{ \AA}, -9 \text{ \AA}, -7 \text{ \AA}, -5 \text{ \AA}, -3 \text{ \AA}, -1 \text{ \AA}$, and 1 \AA). For simulations including a dissolved ion pair, the bias (2) was applied to the anion, while the cation's position was restricted with an additional bias potential,

$$U_{\text{cation}}(\mathbf{r}, z) = c(z_s - (z_{\text{anion}} - z_{\text{cation}}))^2 + d(r_0 - |\mathbf{r}|)^2 \quad (4)$$

where z_s is the desired separation of the cation and anion in the z -direction, \mathbf{r} is the vector pointing from the cation to the anion projected onto the xy -plane, and r_0 is the desired separation in the xy -plane. For the choice of parameters $c = d = 2 \text{ kcal/mol \AA}^2$, $z_s = 3.5 \text{ \AA}$ and $r_0 = 6 \text{ \AA}$, the ions reside in reasonable proximity, both situated near the interface, but separated in the z -direction. Specifically, the anion is confined to $\Delta z_{\text{anion}} \approx -1 \text{ \AA}$ and explores a range of

$\Delta z_{\text{anion}} \pm 1 \text{ \AA}$, while the cation explores a range of depth $\Delta z_{\text{cation}} \approx -5 \text{ \AA}$ and explores a range of Δz_{cation} .

4. Simulation results

4.1. Dilute electrolyte solutions

Single-ion simulations with periodic boundary conditions are in a sense unphysical, since it is not possible in the laboratory to study solutions bearing a macroscopic excess of positive or negative charge. Computer simulations of such systems can nonetheless provide a useful way to understand separately the effects of an anion or cation on its surroundings, and on spectroscopic observables. We also report on electroneutral simulations that include one anion and one cation.

Inspired by simulations and experiments that explore a series of halide ions at the air–water interface, we have investigated F^- , Cl^- , Br^- , and I^- independently as the anionic species. In our simulation models, which lack polarizability, these ions differ essentially only by size. Fig. 1 shows the functions $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ for each of these ions compared to results for a neat water–air system. In all cases, the ion was restrained to a narrow range of depth, $z_{\text{ion}} \approx z_{\text{Gibbs}} - 1 \text{ \AA}$. The most notable aspects of these results are, first, that no substantial new spectroscopic features appear due to ion solvation and, second, that the weak changes we do detect are nearly identical across the halide series. In sharp contrast, halide ion solvation in bulk produces marked Raman shifts, once ascribed to ‘structure making’ or ‘structure breaking’ activity of the ions, but now understood as the consequence of strong electric fields exerted by the anion on adjacent hydroxyl groups [22]. Because those anionic fields decay rapidly over short distances, small ions such as F^- generate distinctly different shifts than do larger ions such as I^- . Such short-ranged, ion-specific modifications are not apparent in the orientational averages we have calculated.

Despite the differing spectroscopic effects of halide ions in the bulk and at the interface, the local solvation structure of each ion is only weakly dependent on depth, within the non-polarizable models we use, for ion positions that occur with appreciable probability [29,30]. We have confirmed this fact by examining, for example, the average number of water molecules in each ion's first solvation shell for $z_{\text{ion}} \leq z_{\text{Gibbs}} + 4 \text{ \AA}$. More pertinently, electric field distributions for protons adjacent to the ion in this depth range are nearly identical to those computed for bulk solutions. The ion-specific frequency shifts that these OH groups experience do not contribute noticeably to computed SFG simply as a consequence of symmetry. Local solvation structure is largely determined by the very strong hydrogen bonds donated by solvent molecules to the anion. For the models we simulate, this local structure does not change substantially in the vicinity of the Gibbs dividing surface [29]. Significant changes do not emerge in the case of iodide solutes until the ion is constrained to reside well above the interface, $z_{\text{ion}} \geq z_{\text{Gibbs}} + 4 \text{ \AA}$. Fluoride anions retain bulk-like first solvation shells even farther into the vapor phase, investigated in our studies up to $z_{\text{ion}} \approx z_{\text{Gibbs}} + 15 \text{ \AA}$. Because the arrangement of solvating molecules in bulk is, on average, symmetric about the ion, its local effects on vibrational frequency are not reflected in $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$.

Though small, the ion-independent changes in orientational averages we have observed can be spectroscopically significant if they occur near the peak of $P(\mathcal{E})$. Both $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ do, in fact, show systematic positive shifts throughout the range $\mathcal{E} < -1 \text{ V/\AA}$. Since these shifts do not arise from directly solvating molecules, they must be longer-ranged in character. We indeed find that ions induce a weak but long-ranged orientational bias on water molecules that extends many molecular diameters into

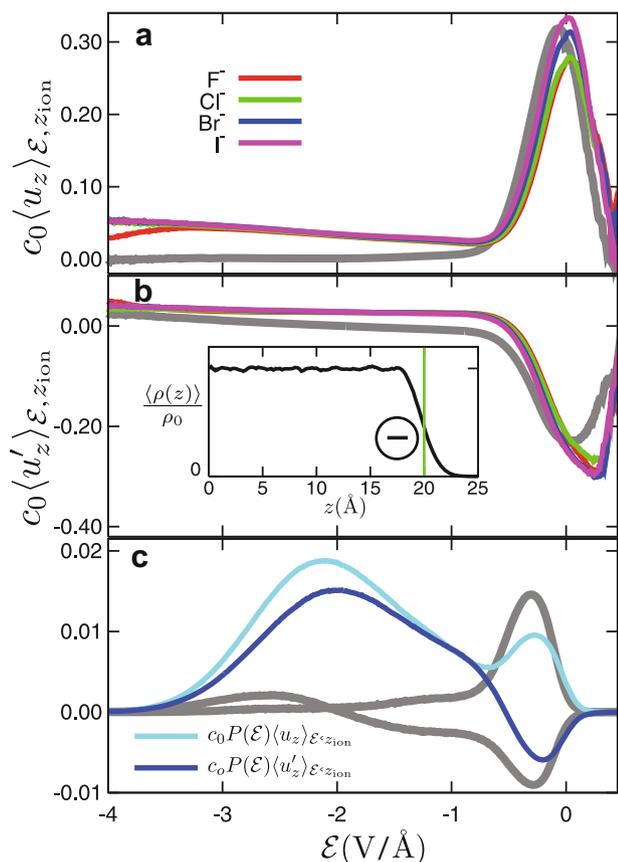


Fig. 1. Average projections of OH and OD bond vectors onto the surface normal for systems including a single anion (and no cation) in the liquid slab. Results for $\langle u_z \rangle_{\mathcal{E}}$ and $\langle u'_z \rangle_{\mathcal{E}}$ for the neat liquid interface are reproduced here (gray curves) for comparison. All orientational averages are multiplied by a factor $c_0 \equiv N/(2L_x L_y) \text{ \AA}^{-2}$ to remove a trivial dependence on system size. Colored lines in (a) and (b) show $c_0 \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $c_0 \langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ for four halide ions: F^- (red), Cl^- (green), Br^- (blue), and I^- (violet). In (c) we plot $c_0 P(\mathcal{E}) \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $c_0 P(\mathcal{E}) \langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ for the Br^- system and $c_0 P(\mathcal{E}) \langle u_z \rangle_{\mathcal{E}}$ and $c_0 P(\mathcal{E}) \langle u'_z \rangle_{\mathcal{E}}$ for the neat liquid (gray). Other anions yield averages indistinguishable from the case of Br^- . In all of these calculations, the ion was restrained to reside close to the interface, with $\langle z_{\text{ion}} \rangle - z_{\text{Gibbs}} = -1.4 \text{ \AA}$ and $\sqrt{\langle (z_{\text{ion}} - \langle z_{\text{ion}} \rangle)^2 \rangle} = 0.5 \text{ \AA}$. The inset in (b) depicts the ion's mean position in relation to the liquid density profile; the Gibbs dividing surface is indicated by the vertical green line. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the slab. This polarization of the subsurface layers has little to do with the ion's size or local solvation structure, arising instead from a weak imbalance in electrostatic forces over the nm scale. The weakness of this effect is evidenced by the nearly frequency-independent offset of $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ due to the ion. Molecular reorientation is so subtle as to be insensitive to its immediate hydrogen bonding environment.

The positive offset of $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ due to weak polarization in the range $\mathcal{E} < -1\text{V}/\text{\AA}$ is accompanied by noticeable frequency dependence. (This function effectively vanishes in neat solvent over the range of frequencies corresponding to hydrogen bond-donating OH groups.) We attribute this additional effect to slight contractions and expansions of the hydrogen bond network radial to the ion: an OH group whose proton is directed toward the ion will experience a force from the ion in that direction (which, for most of the subsurface layer, has a positive projection onto the surface normal). With high probability, its hydrogen bonding partner will reside in roughly the same direction, so that motion toward the ion effects shortening of the hydrogen bond and, as a result, shifting of \mathcal{E} to more negative values. An OH group pointing away from the ion, on the other hand, will tend to retract from its acceptor, generating positive frequency shifts. Computed correlations between r_{OH} , the distance between a proton and its hydrogen bond acceptor, and \mathcal{E} support this picture [18].

Our calculations indicate that the influence of anion solvation, as reflected in orientational averages relevant to SFG, extends over lengths appreciably larger than a molecular diameter. On these scales, the charge asymmetry of a water molecule, which is crucial to hydrogen bonding, no longer dominates solvent response to electrostatic forces. It may therefore not be surprising that the anionic effects discussed above are recapitulated in opposite senses for a single cation at the interface. Fig. 2 shows calculations of $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ from simulations including Na^+ (and no anion) at the interface. Systematic negative shifts over the range $\mathcal{E} < \mathcal{E}^*$, as well as an upward slope, of $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$, can be rationalized using ideas analogous to those we have presented in the context of halide anions.

Any physically realizable electrolyte solution must of course possess both positive and negative ions. At extremely low ionic strength, we could think of such a solution as a concatenation of the single-ion systems we have simulated. We could therefore

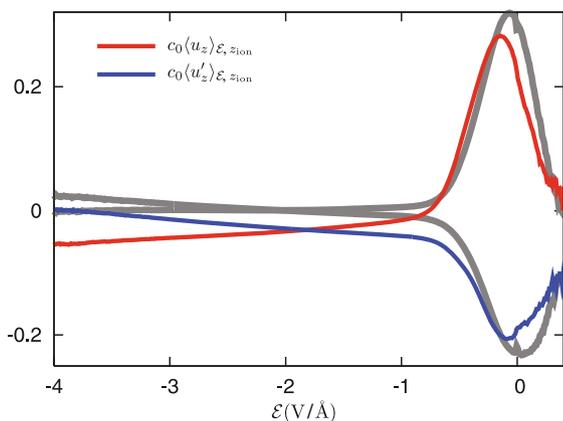


Fig. 2. Average projections of OH and OD bond vectors onto the surface normal for a liquid slab containing a single Na^+ ion (and no anion). As in Fig. 1 and in subsequent figures, the factor $c_0 \equiv N/(2L_x L_y) \text{\AA}^{-2}$ renders the calculated averages as intensive quantities. Results for the neat liquid interface are reproduced here (gray curves) for comparison. Colored lines show $c_0 \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ (red) and $c_0 \langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ (blue) as functions of electric field. As for the anion systems reported in Fig. 1, Na^+ was restrained to reside close to the interface, with $\langle z_{\text{cation}} \rangle - z_{\text{Gibbs}} = -1.3 \text{\AA}$ and $\sqrt{\langle (z_{\text{cation}} - \langle z_{\text{cation}} \rangle)^2 \rangle} = 0.5 \text{\AA}$. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

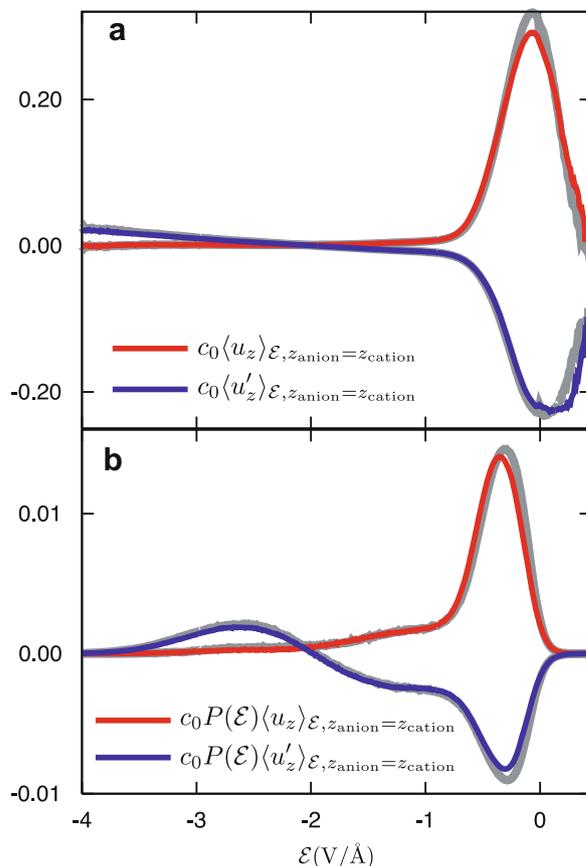


Fig. 3. (color online) Estimate of orientational averages governing SFG response for an ion pair, held at identical depths, at infinite dilution. The plotted data were obtained by averaging calculations for a single dissolved I^- anion with those for a single dissolved Na^+ cation, both held at the same depth (as described in the captions of Figs. 1 and 2). Panel (a) shows $c_0 \langle u_z \rangle_{\mathcal{E}, z_{\text{anion}}=z_{\text{cation}}}$ and $c_0 \langle u'_z \rangle_{\mathcal{E}, z_{\text{anion}}=z_{\text{cation}}}$. In (b) these average projections have been weighted by the electric field distribution in order to highlight close similarity with results for the neat liquid (gray).

approximate the spectroscopic effects of a dissolved ion pair by averaging results obtained for isolated counterions held at the same depth. Fig. 3 shows the results of such a simple-minded average. The individual influences of anion and cation are not only comparable in a qualitative sense; they offset one another quantitatively. This cancellation underscores the long-ranged nature of ionic perturbations manifested in the orientational averages we are considering. Within our approximations, a well-separated pair of ions at the same depth produces no change in SFG susceptibility.

Recent computer simulations have raised the unexpected possibility that simple dissolved ion pairs can establish well defined layers at the air–water interface [3,4]. The effective adsorption of larger halide anions appears to be sensitive to details of intermolecular interactions, and in particular, to ion polarizability, whose effect on SFG we scrutinize closely in Section 4.2. Here we first ask a question that circumvents this sensitivity: With our approximate treatment of SFG and our non-polarizable interaction model, what are the spectroscopic implications of the vertical charge separation predicted by more sophisticated models? Put more simply, do the effects of anion and cation balance fail to cancel when they reside at different depths below the interface?

We have repeated simulations of the single- Na^+ system with the cation restrained to a series of depth intervals. Fig. 4 shows that the ion-induced orientational changes vanish in a smooth and simple way as the ion moves farther into the bulk. Molecular layers above the ion are generally oriented opposite those below the ion, weakening the net polarization until the neat solvent response

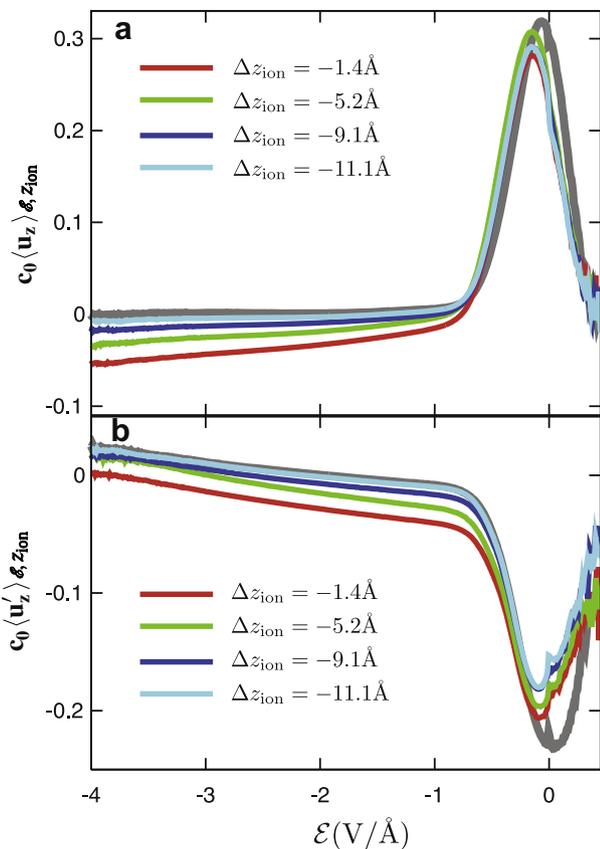


Fig. 4. (color online) Dependence of a liquid slab's orientational bias on the depth of a dissolved cation. Average projections of OH (a) and OD (b) bond vectors onto the surface normal are shown as functions of electric field for a series of systems whose Na^+ cation is restrained to different ranges of $\Delta z_{\text{cation}} = z_{\text{cation}} - z_{\text{Gibbs}}$. In each case $\sqrt{\langle (z_{\text{cation}} - \langle z_{\text{cation}} \rangle)^2 \rangle} = 0.5 \text{ \AA}$. Results for the neat liquid (gray curves) are included for comparison.

is restored. If we repeat the naive averaging procedure to calculate SFG susceptibility for a vertically segregated ion pair, it is clear that the balance of orienting effects will be disturbed, as Fig. 5 confirms. The result is a net change in the functions $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ that, when multiplied by $P(\mathcal{E})$, is considerable. Notably, these modifications to the determinants of second-order susceptibility are similar in form and in magnitude to results obtained from more detailed simulations, as well as from experiment.

We have tested our ideas regarding the opposing influences of an ion pair by performing simulations that include both Na^+ and I^- . Here we probe an extreme that complements our treatment of infinite dilution, in which the two ions are held close together in a configuration chosen to mimic the density profiles of high concentration electrolyte solutions where ion layering is evident. Fig. 6 demonstrates that our result for the dilute limit provides a surprisingly accurate estimate for the case of paired ions.

4.2. Effect of ion polarizability on SFG

Omitting anion polarizability is a potentially serious shortcoming of the molecular model used in the preceding sections to examine SFG response at electrolyte–vapor interfaces. Using computer simulations, Tobias and coworkers have shown that the attraction for the interface of larger halide anions such as I^- is substantially weakened when their dipole fluctuations are neglected [4]. The solvation effects underlying strong charge layering (which does not occur in our non-polarizable model) could also introduce pro-

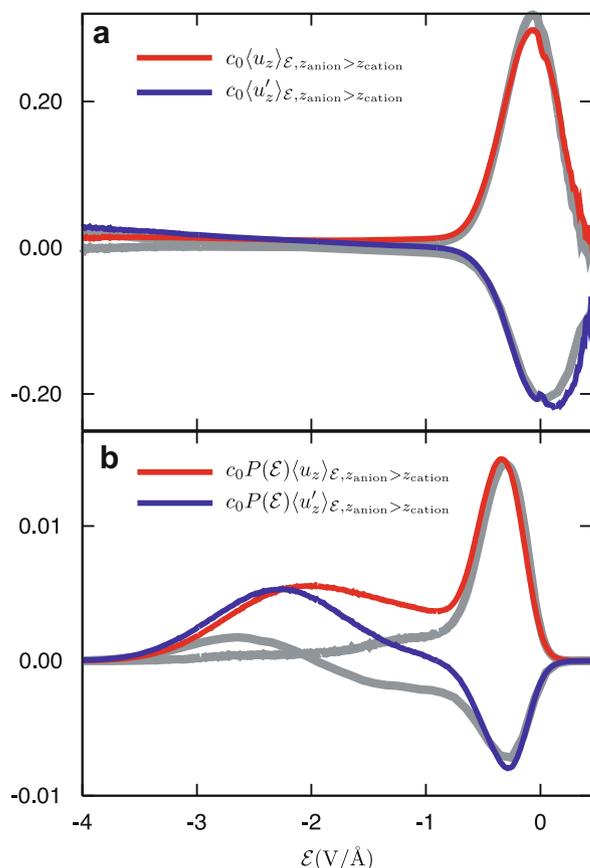


Fig. 5. (color online) Estimate of orientational averages governing SFG response for a stratified ion pair at infinite dilution. The plotted data were obtained by averaging calculations for a single dissolved I^- anion, held at depth $\langle \Delta z_{\text{anion}} \rangle = -1.2 \text{ \AA}$, with calculations for a single dissolved Na^+ cation, held at lower depth $\langle \Delta z_{\text{cation}} \rangle = -7.1 \text{ \AA}$. Depth of both ions was allowed to fluctuate by $\sqrt{\langle (z_{\text{ion}} - \langle z_{\text{ion}} \rangle)^2 \rangle} = 0.5 \text{ \AA}$. Panel (a) shows $c_0 \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $c_0 \langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$. In (b) these average projections have been weighted by the electric field distribution in order to highlight differences with results for the neat liquid (gray).

nounced asymmetry in an ion's first coordination shell [31]. In that case, the longer-ranged contributions we have described would be supplemented, or perhaps even outweighed, by orientation and frequency shifts of hydroxyl groups adjacent to the ion.

We have examined the possible importance of induced solute dipoles by computing the orientational averages $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ for a polarizable ion held fixed at a series of depths below the interface, i.e., we have determined the effects of polarizability on the conditional averages $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$. From these quantities, SFG susceptibility can be calculated using

$$\text{Im} \beta_{\text{xxz}}^{(\text{R})}(\omega) = \frac{\pi}{Q} \int dz_{\text{ion}} p(z_{\text{ion}}) P(\mathcal{E}|z_{\text{ion}}) \sum_{j,k,l} \alpha'_{jk} \mu'_l \langle j_x k_x l_z \rangle_{\mathcal{E}, z_{\text{ion}}} \quad (5)$$

At the ion concentrations of our simulations, the dependence of $P(\mathcal{E}|z_{\text{ion}})$ on ion depth is undetectable. We can thus safely write the hyperpolarizability as a linear combination of spatially averaged functions $\int dz_{\text{ion}} p(z_{\text{ion}}) \langle j_x k_x l_z \rangle_{\mathcal{E}, z_{\text{ion}}}$, and subsequently in terms of the simpler quantities $\int dz_{\text{ion}} p(z_{\text{ion}}) \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\int dz_{\text{ion}} p(z_{\text{ion}}) \langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$. This simplification accomplishes a separation of two distinct effects of ion polarizability. The first, which has been widely discussed, is a spatial redistribution of ion depths described by changes in $p(z_{\text{ion}})$. Here we exclusively consider the second effect, namely, changes, due to polarizability, in the orientational averages $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}$ when ion depth is restrained.

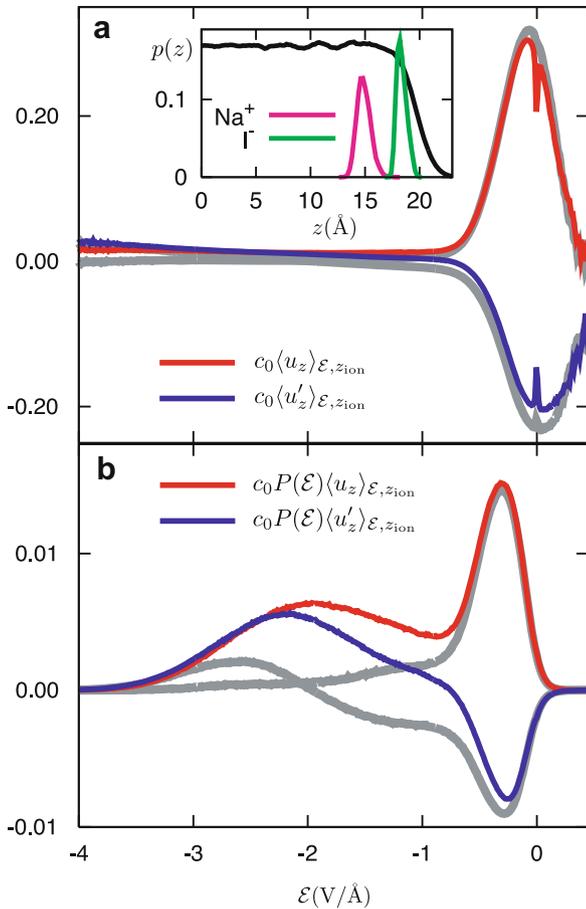


Fig. 6. Average projections of OH and OD bond vectors onto the surface normal for a liquid slab containing a pair of ions held at different depths, but in close proximity, near the interface. Subject to the bias potentials described in the text, the I^- anion fluctuates about a mean depth $\langle \Delta z_{\text{anion}} \rangle = -1.5 \text{ \AA}$ by an amount $\sqrt{\langle (z_{\text{anion}} - \langle z_{\text{anion}} \rangle)^2 \rangle} = 0.5 \text{ \AA}$. The Na^+ cation resides at a mean depth $\langle \Delta z_{\text{cation}} \rangle = -5 \text{ \AA}$ and undergoes vertical fluctuations of size $\sqrt{\langle (z_{\text{cation}} - \langle z_{\text{cation}} \rangle)^2 \rangle} = 0.7 \text{ \AA}$. Orientational averages $c_0 \langle u_z \rangle_{\mathcal{E}}$ (red) and $c_0 \langle u'_z \rangle_{\mathcal{E}}$ (blue) are shown in (a); their weighted counterparts $c_0 P(\mathcal{E}) \langle u_z \rangle_{\mathcal{E}}$ and $c_0 P(\mathcal{E}) \langle u'_z \rangle_{\mathcal{E}}$ are shown in (b). Results for the neat liquid (gray) are included for comparison. The inset in (a) depicts the solvent density profile (scaled by an arbitrary constant) as well as distributions of depth $p(z)$ for the two ions. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

To assess such consequences of ion polarizability, we introduce the solute's dipole $\boldsymbol{\mu}$ as a dynamical variable, and supplement the potential energy studied in previous sections, $U^{(0)}$, with terms regulating fluctuations in $\boldsymbol{\mu}$:

$$U^{(\text{pol})} = U^{(0)} - \boldsymbol{\xi}_{\text{ion}} \cdot \boldsymbol{\mu} + \frac{|\boldsymbol{\mu}|^2}{2\alpha}. \quad (6)$$

Here, α is the ion polarizability, and vector $\boldsymbol{\xi}_{\text{ion}}$ is the instantaneous electric field exerted by the solution on the ion. Note that $\boldsymbol{\xi}_{\text{ion}}$ is a function of all particle positions.

We compute averages over the Boltzmann distribution defined by Eq. (6) using its non-polarizable counterpart as a reference system. Integrating out fluctuations in $\boldsymbol{\mu}$, we obtain for an arbitrary observable quantity A

$$\langle A \rangle^{(\text{pol})} = \frac{\langle A \exp(\beta \alpha \xi^2 / 2) \rangle^{(0)}}{\langle \exp(\beta \alpha \xi^2 / 2) \rangle^{(0)}}, \quad (7)$$

where $\xi \equiv |\boldsymbol{\xi}_{\text{ion}}|$. Superscripts '(pol)' and '(0)' denote averages over fluctuations in the polarizable and non-polarizable systems, respectively. For one of the orientational averages relevant to SFG, we have specifically

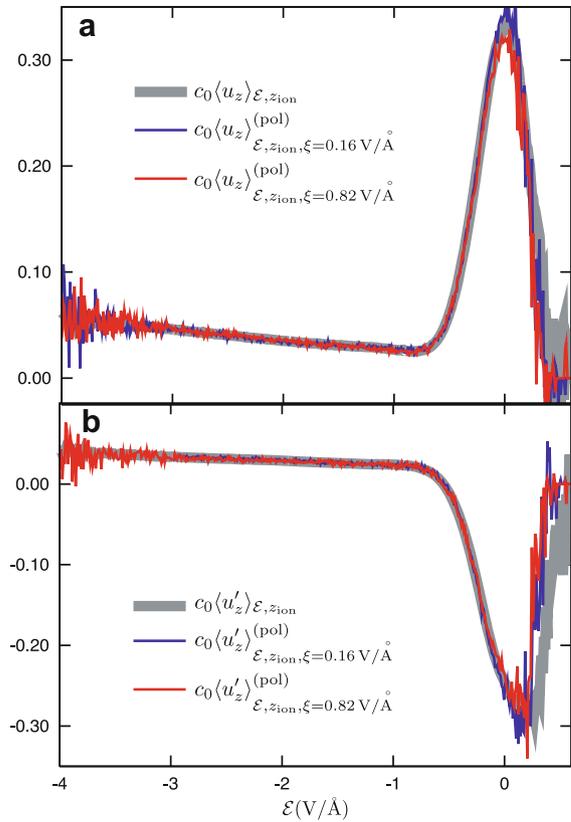


Fig. 7. Influence of dipole induction on orientational averages when a single I^- anion is held fixed at depth $\langle \Delta z_{\text{anion}} \rangle = -1.3 \text{ \AA}$ with vertical fluctuations of size $\sqrt{\langle (z_{\text{anion}} - \langle z_{\text{anion}} \rangle)^2 \rangle} = 0.5 \text{ \AA}$. Red and blue curves show the conditional averages $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(0)}$ and $\langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(0)}$ for two extreme values of the electric field ξ acting on the ion (which determines dipole induction). For comparison, we reproduce the results from Fig. 1 for a non-polarizable iodide anion (gray curves). The thermal distribution of ξ in these circumstances includes 93% of its weight between $\xi = 0.16 \text{ V/\text{\AA}}$ (blue curves) and $\xi = 0.82 \text{ V/\text{\AA}}$ (red curves). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

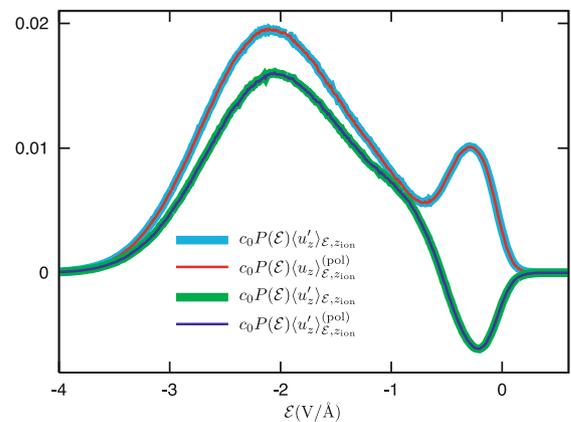


Fig. 8. Weighted orientational averages, $P(\mathcal{E}) \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(\text{pol})}$ and $P(\mathcal{E}) \langle u'_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(\text{pol})}$, underlying SFG response for a polarizable iodide anion held at $\langle \Delta z_{\text{anion}} \rangle = -1.3 \text{ \AA}$ with $\sqrt{\langle (z_{\text{anion}} - \langle z_{\text{anion}} \rangle)^2 \rangle} = 0.5 \text{ \AA}$. Plotted results (blue and red curves) were calculated from Eq. (8) with polarizability $\alpha = 6.92 \text{ \AA}^3$ [24]. For comparison we reproduce the results from Fig. 1 for a non-polarizable iodide anion (cyan and green curves). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

$$\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(\text{pol})} = \frac{\int d\xi \exp(\beta \alpha \xi^2 / 2) P^{(0)}(\mathcal{E}, z_{\text{ion}}, \xi) \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}, \xi}^{(0)}}{\int d\xi \exp(\beta \alpha \xi^2 / 2) P^{(0)}(\mathcal{E}, z_{\text{ion}}, \xi)}. \quad (8)$$

(Results for the other key orientational average $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(\text{pol})}$ yield conclusions analogous to those drawn below.) We have defined $P^{(0)}(\mathcal{E}, z_{\text{ion}}, \xi)$ as the joint probability distribution for equilibrium fluctuations of ξ (the magnitude of the solution's electric field acting on the ion), \mathcal{E} , and z_{ion} in the non-polarizable ensemble.

Fig. 7 shows simulation results for $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}, \xi}^{(0)}$ as a function of \mathcal{E} , for an iodide anion held at $z_{\text{ion}} = 19 \text{ \AA} \pm 1 \text{ \AA}$ (using the bias potentials discussed in Section 3) and for values of ξ spanning the range of typical equilibrium fluctuations. The profound insensitivity to ξ evident in these data, especially in the hydrogen bonding region of \mathcal{E} , are representative of simulations we have performed for a variety of ion depths and identities. This fact, together with Eq. (8), suggests that $\langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(\text{pol})} = \langle u_z \rangle_{\mathcal{E}, z_{\text{ion}}}^{(0)}$ to an excellent approximation. Carrying out the integrations in Eq. (8) numerically, we indeed find negligible differences between these quantities, as shown in Fig. 8.

For the molecular models under consideration, the influence of ion polarizability lies almost entirely in modifying the spatial distributions $p(z_{\text{ion}})$. The statistics of electric field fluctuations that modulate OH stretching frequency are nearly identical in polarizable and non-polarizable models when the ion depth is restrained. These results provide strong justification for the approach we have adopted in previous sections, and for the conclusion that ion-specific aspects of SFG have little to do with local solvation structure.

5. Conclusions

We have shown that ion-specific effects on SFG spectra in sodium halide solutions can have very different origins than those observed in bulk Raman spectra. Frequency shifts for OH groups proximal to the ion, which dominate changes in bulk spectra [22], have little influence on SFG response due to the nearly symmetric organization, on average, of an anion's nearby solvation structure. For the molecular model we have studied, the interface has little influence on these local solvent geometries. When placed at the same depths, all halide ions we have studied affect relevant orientational averages in precisely the same way, reflecting weak, long-ranged polarization of subsurface layers. Since cations induce an exactly opposing response, these effects would not be noticeable on macroscopic scales in a neutral solution whose cation and anion density profiles are identical. This conclusion is robust to the inclusion of dipole induction on polarizable anions.

Noticeable spectroscopic influence of dissolved salts might instead arise from the specific way charged solutes are distributed in space relative to the interface. We have shown that computed SFG response is, in fact, sensitive to the kind of charge layering suggested by previous simulation studies for larger halide anions. As a result, spectroscopic ion specificity at the interface could well reflect variations in surface density profiles across the halide series.

Acknowledgements

This work was supported by the Director, Office of Science, Office of Basic Energy Sciences, Materials Sciences and Engineering Division, of the US Department of Energy under Contract No. DE-AC02-05CH11231. The authors also thank Rich Saykally for useful discussions.

References

- [1] D. Liu, G. Ma, L. Levering, H. Allen, J. Phys. Chem. B 108 (2004) 2252.
- [2] P. Petersen, R. Saykally, Chem. Phys. Lett. 397 (2004) 51.
- [3] P. Jungwirth, D.J. Tobias, J. Phys. Chem. B 105 (2001) 10468.
- [4] P. Jungwirth, D.J. Tobias, J. Phys. Chem. B 106 (2002) 6361.
- [5] L. Vrbka, M. Mucha, B. Minofar, P. Jungwirth, E. Brown, D. Tobias, Curr. Opin. Colloid Interface Sci. 9 (2004) 67.
- [6] L. Onsager, N. Samaras, J. Chem. Phys. 2 (1934) 528.

- [7] A.A. Rashin, B. Honig, J. Phys. Chem. 89 (1985) 5588.
- [8] J. Cheng, C. Vecitis, M. Hoffmann, A. Colussi, J. Phys. Chem. B (Lett.) 110 (2006) 25598.
- [9] L.M. Pegram, J.M. Thomas Record, J. Phys. Chem. B 111 (2007) 5411.
- [10] S. Ghosal et al., Science 307 (2005) 563.
- [11] P.B. Petersen, R.J. Saykally, Annu. Rev. Chem. 57 (2006) 333.
- [12] E.A. Raymond, G.L. Richmond, J. Phys. Chem. B 108 (2004) 5051.
- [13] A. Morita, J.T. Hynes, Chem. Phys. 258 (2000) 371.
- [14] A. Morita, J.T. Hynes, J. Phys. Chem. B 106 (2002) 673.
- [15] J.L. Skinner, personal communication, 2008.
- [16] E.C. Brown, M. Mucha, P. Jungwirth, D.J. Tobias, J. Phys. Chem. B 109 (2005) 7934.
- [17] V. Buch, T. Tarbuck, G.L. Richmond, H. Groenzin, I. Li, M.J. Shultz, J. Chem. Phys. 127 (2007) 204710.
- [18] J. Noah-Vanhoucke, J.D. Smith, and P.L. Geissler, J. Phys. Chem. B (2009), accepted for publication.
- [19] J.D. Smith, C.D. Cappa, K.R. Wilson, R.C. Cohen, P.L. Geissler, R.J. Saykally, Proc. Natl. Acad. Sci. USA 102 (2005) 14171.
- [20] P.L. Geissler, J. Am. Chem. Soc. 127 (2005) 14930.
- [21] J.D. Eaves, A. Tokmakoff, P.L. Geissler, J. Phys. Chem. A 109 (2005) 9424.
- [22] J.D. Smith, R.J. Saykally, P.L. Geissler, J. Am. Chem. Soc. 129 (2007) 13847.
- [23] H.J. Berendsen, J.R. Grigera, T.P. Straatsma, J. Phys. Chem. 91 (1987) 6269.
- [24] L.X. Dang, J. Phys. Chem. B 106 (2002) 10388.
- [25] S. Plimpton, J. Comput. Phys. 117 (1) (1995), <<http://lammps.sandia.gov>>.
- [26] J.-P. Ryckaert, G. Ciccotti, H.J. Berendsen, J. Comput. Phys. 23 (1977) 327.
- [27] W.G. Hoover, Phys. Rev. A 31 (1985) 1695.
- [28] W.C. Swope, H.C. Andersen, J. Chem. Phys. 76 (1982) 637.
- [29] I. Benjamin, J. Chem. Phys. 95 (1991) 3698.
- [30] M.A. Wilson, A. Pohorille, J. Chem. Phys. 95 (1991) 6005.
- [31] P. Jungwirth, D.J. Tobias, Chem. Rev. 106 (2006) 1259.



Joyce Noah-Vanhoucke received her B.S. degree in chemistry with minors in mathematics and computer science from New York University in 2001, where she worked with Tamar Schlick. Working with Hans C. Andersen, she received a Ph.D. from Stanford University in 2006, where she was also a recipient of the Department of Energy Computational Science Graduate Fellowship. She is currently a post-doctoral research associate at the University of California, Berkeley, working with Phillip Geissler. Her current interests include the electric field statistics which form the basis of the work described here as well as the broader phenomenon of ion solvation at interfaces.



Jared D. Smith Born in Little Rock, Arkansas, Jared received his bachelor's degree in chemistry in 2001 from Portland State University, in Portland Oregon, where he worked with Prof. Dean Atkinson. He then moved to Sandia National Laboratory in California for a year long internship with Craig Taatjes. He remained in the bay area for graduate school, and received his Ph.D. in 2006 from the University of California, Berkeley under the supervision of Richard Saykally. He is currently a Dreyfus Environmental Postdoctoral Fellow working with Kevin Wilson and Steve Leone at the Lawrence Berkeley National Laboratory.



Phillip Geissler Born in Ithaca, New York, in 1974 and raised in Virginia, Phillip Geissler returned to his natal roots as an undergraduate at Cornell University. He received his Ph.D. at the University of California, Berkeley, in 2000, working with David Chandler. Geissler pursued postdoctoral research at Harvard with Eugene Shakhnovich, and at MIT as a Science Fellow. He returned to his western roots in 2003, joining the faculty at UC Berkeley as a professor of chemistry. Geissler's research group develops and applies theoretical tools of statistical mechanics to explore emergent molecular behavior in complex chemical and biophysical materials. This work has been recognized by fellowships from the Packard and Sloan Foundations and by an award from the Hellman Faculty Fund.